

# A protocol synthesis method for fault-tolerant multipath routing

K. Ishida<sup>a,\*</sup>, Y. Kakuda<sup>a</sup>, M. Nakamura<sup>b</sup>, T. Kikuno<sup>b</sup>, K. Amano<sup>a</sup>

<sup>a</sup>Faculty of Information Sciences, Hiroshima City University, Asaminami-ku, Hiroshima, 731-3194, Japan

<sup>b</sup>Graduate School of Engineering Science, Osaka University, Toyonaka-shi, Osaka, 560-8531, Japan

## Abstract

This paper proposes a new synthesis method for generating fault-tolerant multipath routing protocols. The protocol is defined as fault-tolerant if messages can be rerouted by using another path when a communication channel fails. The routing protocols obtained adopt a multipath routing function, augmented with routing table, where each table stores the next nodes for multipath routing, and updates the tables according to the network topology changes. Additionally, the routing protocol can attain flexibility by the multipath routing mechanism in the sense that only a small amount of change is needed for the change of network topology. We also briefly describe an extension of the proposed method for generating multicast routing protocols. © 1999 Elsevier Science B.V. All rights reserved.

*Keywords:* Protocol engineering; Protocol synthesis; Multipath routing; Fault-tolerant routing; Flexible routing

## 1. Introduction

Routing in a packet-switched network is to deliver packets through communication paths from a source node to a destination node. The multipath routing is more robust than single path routing because as long as at least one of the multiple paths between source and destination nodes is viable the messages will be delivered. Multipath routing is thus one of the most promising ways to realize the reliable routing services [1,2].

The most fundamental requirement for multipath routing protocols is considered as follows [3]:

### Requirement 1

Fundamental capability for multipath routing. As messages are delivered through multiple communication paths, protocol specification for the message delivery must be specified for any node on the communication paths. Next, fault-tolerance and flexibility become important characteristics to ensure quality of communication services. Therefore, the protocol must also satisfy the following two hard requirements.

### Requirement 2

Fault-tolerance for a communication channel failure. In order to definitely deliver messages from source node to destination node even when a communication channel fails, the source node must possess a recovery function of rerouting.

### Requirement 3

Flexibility for network topology changes. When some nodes and channels are newly added or deleted on the network, modification of the protocol specification must be easily done.

Design of practical multipath routing protocols is complex and difficult due to the complicated requirements listed above. For such a difficult and complex protocol design, the protocol synthesis [4,5] is recognized as one of the most prominent solutions, which automatically derives the protocol specifications without specification errors. In this paper, a synthesis of multipath routing protocols is defined as the generation of a routing protocol specification from a routing service specification, both of which are modeled by Finite State Machines (FSMs). So far, various protocol synthesis methods have been proposed [4–7]. However, none of them were for routing protocols with recovery function of rerouting, although the previous methods generate recovery functions such as retransmission for message loss, check pointing and roll-back recovery for coordination loss [8,9].

This paper proposes a new synthesis method for complex multipath routing protocols, which satisfy Requirements 1, 2 and 3. The proposed method generates multipath routing augmented with routing table. Each table stores the candidates of the next nodes. The table is utilized for determining the next node to which messages are transmitted along a communication path. The synthesized protocol specification has a rerouting function, such that the messages can be rerouted through one of the multiple paths by referring the table. Moreover, the protocol specification can be modified

\* Corresponding author.

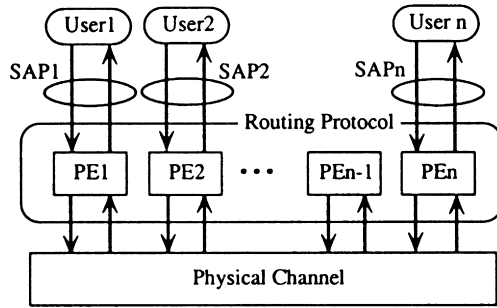


Fig. 1. Communication model.

easily by updating the table, even if network topology changes.

The rest of this paper is organized as follows: Section 2 gives fundamental definitions concerning protocol synthesis. In Section 3, we define synthesis problem for multipath routing and propose a solution to the problem. Then, we prove the correctness of the method in Section 4, and apply our method to a typical example in Section 5. Flexibility for topology change and an extension for multicast routing are discussed in Section 6. Finally, Section 7 concludes this paper.

## 2. System model

### 2.1. Communication model

As shown in Fig. 1, a communication service is specified by service primitives exchanged between users in the higher layer, and nodes in the lower layer through service access points (SAPs). A routing protocol can be viewed as a black box from the users' view point. The nodes are also called protocol entities, which are denoted by PEs in the following. As the users correspond to protocol entities in the higher layer, it is assumed that one user uses one PE. In a routing protocol, each PE must deliver a message through existing physical channels.

### 2.2. Topology graph

**Definition 1.** A topology graph is defined as an undirected graph  $G = (V, E)$ , where  $V$  represents a set of PEs, and  $E (\subseteq V \times V)$  represents a set of communication channels (FIFO queues).

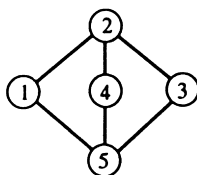


Fig. 2. A topology graph.

For any two nodes,  $PE_u, PE_v \in V$  on a topology graph  $G = (V, E)$ , if there exists an edge  $(u, v) \in E$ , then node  $PE_u$  is called an adjacent node of  $PE_v$ . Fig. 2 shows a topology graph. This paper imposes the following restriction to assure the connectivity of the communication path between any pair of PEs even if a communication channel fails.

**Restriction 1.** There are at least two edge-disjoint undirected paths between any two PEs in the topology graph.

From Restriction 1, for any pair of nodes  $PE_i, PE_j \in V$ , a path  $\rho$  between  $PE_i$  and  $PE_j$  must exist. Intuitively, the path can be interpreted as a communication path from protocol entities  $PE_i$  to  $PE_j$ . Let us consider a case that  $user_i$  communicates with  $user_j$  via the path. At first,  $user_i$  sends the service primitive  $p$  to  $PE_i$ . Next,  $PE_i$  sends a message  $e$  to  $PE_j$  via the path. Then,  $PE_j$  receives  $e$  and sends the service primitive  $q$  to  $user_j$ . For this, we call  $PE_i$  and  $PE_j$ , *S-node* and *D-node* of the path, respectively. For the path, the intermediate nodes between  $PE_i$  and  $PE_j$  are called *R-nodes* on  $\rho$ . Messages are delivered from the *S-node* to the *D-node* via *R-nodes* on the communication path. As a special case, if  $PE_i$  is an adjacent node of  $PE_j$  and  $\rho = (PE_i, PE_j)$ , then  $\rho$  does not have an *R-node*.

### 2.3. Service specification

A service specification defines an execution order of service primitives that are exchanged between users and PEs through service access points. A service access point (SAP), between  $user_i$  and  $PE_i$ , is denoted by  $SAP_i$ .

**Definition 2.** A service specification is modeled by an FSM,  $S = \langle S_s, \Sigma_s, T_s, \sigma \rangle$ , where

- $S_s$  is a non-empty finite set of service states.
- $\Sigma_s$  is a finite set of service primitives. Each service primitive  $p \in \Sigma_s \cup \{\varepsilon\}$  has, as an attribute, an index of SAP through which  $p$  passes, and  $\varepsilon$  is a null primitive that causes no message exchange. When  $p$  passes through  $SAP_i$ , we define a function  $sap(p) = i$ , and the primitive is denoted by  $p_i$ .
- $T_s: S_s \times \Sigma_s \rightarrow S_s$  is a partial transition function. For simplicity, we use  $T_s$  also to represent a set of triplets  $(u, p, v)$ , such that  $v = T_s(u, p)$  ( $u, v \in S_s$ ).
- $\sigma \in S_s$  is an initial service state.

A state  $u \in S_s$  is called a final state iff there is no outgoing transition  $(u, p, v)$  for any  $p$  and  $v$ . If more than one transition is outgoing from a service state, one such transition is chosen and executed. We call this FSM a service specification S-SPEC. An S-SPEC is represented by a labeled directed graph. For any state which represents a service state  $s \in S_s$  in  $S$ , we define  $OUT(S) = \{i | i = sap(p)\}$ , where  $p$  is a label attached to an outgoing transition from  $s$ .

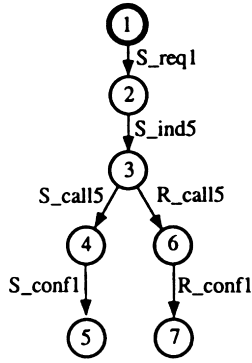


Fig. 3. An example of service specification S-SPEC.

**Example 1.** An example of the S-SPEC is shown in Fig. 3. In this figure, a circle denotes a service state, and an arrow denotes a transition between states. The state drawn by a bold circle is an initial state. This service specification represents sequences of message delivery from the source node to the destination node and its positive or negative acknowledgement from the destination node to the source node. For example, after  $user_1$  sends  $S\_req1$  to  $PE_1$  through  $SAP_1$ ,  $user_5$  receives  $S\_ind5$  from  $PE_5$  through  $SAP_5$  in this order. In  $user_5$  sends  $S\_call5$  (ACK) through  $SAP_5$ ,  $user_1$  receives  $S\_conf1$  from  $PE_1$  through  $SAP_1$ . In case  $user_5$  sends  $R\_call5$  (NACK) through  $SAP_5$ ,  $user_1$  receives  $S\_conf1$  from  $PE_1$  through  $SAP_1$ .

This paper additionally imposes the following restrictions to assure the correctness of the proposed protocol synthesis method.

**Restriction 2.** Consider an S-SPEC and any transition sequence  $(u_1, p_1, u_2), (u_2, p_2, u_3) \dots (u_k, p_k, u_{k+1})$  in the S-SPEC, where  $u_1$  is the initial state and  $u_{k+1}$  is a final state in the S-SPEC. There exists an execution order of service primitives  $p_1, p_2, \dots, p_k$ , such that service primitive  $p_i (i \leq k)$  must be executed before service primitives  $p_{i+1}, p_{i+2}, \dots, p_k$  for any  $i$ .

**Restriction 3.** In S-SPEC, for any three states  $u, v$ , and  $w (v \neq w)$ ,  $T_s$  does not include two transitions  $(u, p, v)$ ,  $(u, p', w)$  with  $sap(p) \neq sap(p')$  and  $p \neq p'$ .

This restriction implies that service primitives  $p$  and  $p'$  are not simultaneously exchanged through different SAPs.

#### 2.4. Protocol specification

The protocol specification consists of  $n$ -tuples of specifications for PEs. In order to realize loop-free transmission, we assume that after a message is received from the adjacent  $PE_i$ , it cannot be transmitted to the same  $PE_i$ . Transmission

and reception of messages between adjacent nodes are defined as follows:

**Definition 3.** If a message  $e$  is transmitted to  $PE_j$ , then it is denoted by a transmission event  $!e(j)$ . On the contrary, if a message  $e$  is received by  $PE_j$ , then it is denoted by a reception event  $?e(j)$ . If the message  $e$  is transmitted to (or received by) one of  $PE_{j_1}, PE_{j_2}, \dots, PE_{j_k}$ , it is denoted by a transmission event  $!e(j_1, j_2, \dots, j_k)$  (or  $?e(j_1, j_2, \dots, j_k)$ ), respectively.

We introduce a set of nodes called routing table  $t$ -set for each node  $PE_i$ . The  $t$ -set is used for determining the adjacent node to which the  $PE_i$  transmits or receives messages along a communication path. The transmission event  $!e(t\text{-set})$ , where  $t\text{-set} = \{j_1, j_2, \dots, j_k\}$  implies that message  $e$  is transmitted to one of the adjacent nodes  $PE_{j_1}, PE_{j_2}, \dots, PE_{j_k}$ . A reception event  $?e(j_1, j_2, \dots, j_k)$  is also denoted by  $?e(t\text{-set})$  with the  $t$ -set. It is assumed that the adjacent nodes are determined by the  $S$ -node of message  $m$  and the identification number of the communication path on which message  $m$  is delivered. This is the so-called source-based routing.

**Definition 4.** A PE specification is modeled by an FSM  $P_i = \langle S_{ip}, \Sigma_{ip}, T_{ip}, \sigma_{ip} \rangle$ , where

- $S_{ip}$  is a non-empty finite set of protocol states.
- $\Sigma_{ip}$  is a non-empty finite set of protocol events.  $\Sigma_{ip} = \{p | p \in \Sigma_s, sap(p) = i\} \cup MEX_i \cup \{T.O.\} \cup \{\varepsilon\}$ , where  $\Sigma_s$  is a set of primitives in Definition 2, and  $MEX_i$  is a set of events which are transmitted to  $PE_{i_1}, PE_{i_2}, \dots, PE_{i_k}$  or received by  $PE_{i_1}, PE_{i_2}, \dots, PE_{i_l}$  and T.O. is a timeout event that occurs when a predetermined time elapses.  $\varepsilon$  is null primitive that causes no message exchanging.
- $T_{ip} : S_{ip} \times \Sigma_{ip} \rightarrow S_{ip}$  is a partial transition function.
- $\sigma \in S_{ip}$  is an initial protocol state.

We call this FSM a PE-SPEC $_i$ . As with the service specification, a PE specification is also represented by a labeled directed graph. We explain a timeout transition  $(u, T.O., v)$  in  $T_{ip}$ . At the time when the state of PE-SPEC $_i$  moves the state  $u$ , counting time starts. Only when a current state of PE-SPEC $_i$  is state  $u$  and the predetermined time elapsed, the state of PE-SPEC $_i$  moves the state  $v$ . A state  $u \in S_{ip}$  is called a final state iff there is no outgoing transition  $(u, p, v)$  for any  $p$  and  $v$ . A state  $u \in S_{ip}$  is called a receiving state for  $e$  iff any (outgoing or incoming) transition from  $u$  is a reception event  $(u, e, v)$  for any  $e$  and  $v$ . A transition “ $p/q$ ” with  $p, q \in T_p$  denotes a successive execution of transitions  $p$  and  $q$ .

**Example 2.** Fig. 4 shows an example of PE-SPEC $_1$  for  $PE_1$  in Fig. 2. In this figure, a circle denotes a protocol state, and an arrow between states denotes a transition.

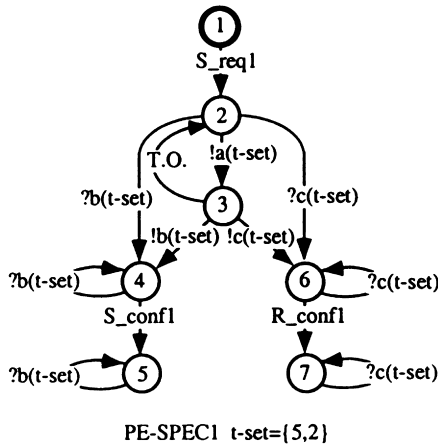


Fig. 4. An example of protocol entity specification.

For example,  $!a(t\text{-set})$ , where  $t\text{-set} = \{5,2\}$  implies two possible message transmissions  $!a(5)$  and  $!a(2)$ .

The following definition requires that messages are exchanged through existing channels.

**Definition 5.** Consider a topology graph  $G = (V,E)$  and a PE specification  $P_i = \langle S_{ip}, \Sigma_{ip}, T_{ip}, \sigma_{ip} \rangle$ . Transitions  $(u,!e(j),v)$  and  $(u,?e(j),v)$  in  $T_{ip}$  obey channel restriction if the following conditions are satisfied, respectively.

If  $(i,j) \notin E'$ , then  $(u,!e(j),v) \notin T_{ip}$  for any  $u, v, e$ , and if  $(i,j) \in E'$ , then  $(u,?e(j),v) \notin T_{ip}$  for any  $u, v, e$ .

If all transitions in  $T_{ip}$  obey channel restriction, we say  $P_i$  obeys channel restriction. And if all  $P_i$ s obey channel restriction, we say  $P$  obeys channel restriction.

### 3. Synthesis method for fault-tolerant multipath routing

#### 3.1. Protocol synthesis problem

Protocol synthesis problem for fault-tolerant multipath

routing to be solved in this paper is formally defined as follows:

**Problem FM.** *Input:* A topology graph  $G$  with Restriction 1, and a service specification  $S$  with Restrictions 2 and 3. *Output:* A multipath routing protocol specification  $P$  which satisfies the following Conditions. *Condition 1:* Unspecified receptions never occur in  $P$ . *Condition 2:* Even if a message loss occurs, the execution order of service primitives defined by  $S$  is kept in  $P$ . *Condition 3:*  $P$  obeys the channel restriction.

No existence of unspecified receptions in Condition 1, and keeping execution order of service primitives in Condition 2 are ordinary conditions for protocol synthesis. Meanwhile, the channel restriction in Condition 3 and discussions on the failure of communication channel in Condition 2 are unique to our discussion. Requirements 1–3 in Section 1 are taken into consideration as above Conditions 1–3.

#### 3.2. Outline of the synthesis method

For Problem FM, the proposed method to derive a protocol specification from a given service specification consists of the following four steps:

- Step 1 Obtain  $n$  projected service specifications by applying the projection to the given service specification S-SPEC. In these projected service specifications, the service primitive associated with  $SAP_i$  is represented by PS-SPEC $_i$ , which is obtained from S-SPECs by substituting each transition not associated with  $SAP_i$  by  $\epsilon$ .
- Step 2 Construct PE-SPEC $_i$  by applying the transition synthesis rules shown in Fig. 5 to PS-SPEC $_i$  obtained in Step 1. In Fig. 5,  $OUT$  is specified in Section 2.3, and  $E_i$  denotes a service primitive in the PS-SPEC $_i$ . Each pair of transition synthesis rules  $A_k$  and  $B_k$  ( $k = 1,2$ ) is applied to each pair of transitions  $(S_1, E_i, S_2)$  in PS-SPEC $_i$  and  $(S_1, \epsilon, S_2)$  in PS-SPEC $_j$  ( $i \neq j$ ), respectively. Message  $e$  is

	Input	Condition	Output
A1	$s_1 \xrightarrow{E_i} s_2$ PS-SPEC $i$	Out( $s_2$ ) = $\{i\}$	$s_1 \xrightarrow{E_i} s_2$ PS-SPEC $i$
B1	$s_1 \xrightarrow{\epsilon} s_2$ PS-SPEC $j$ ( $j \neq i$ )		$s_1 \xrightarrow{\epsilon} s_2$ PS-SPEC $j$ ( $j \neq i$ )
A2	$s_1 \xrightarrow{E_i} s_2$ PS-SPEC $i$	Out( $s_2$ ) $\neq \{i\}$	$s_1 \xrightarrow{E_i/!e(x)} s_2$ $x = Out(s_2)$ PS-SPEC $i$
B2	$s_1 \xrightarrow{\epsilon} s_2$ PS-SPEC $j$ ( $j \neq i$ )		$s_1 \xrightarrow{?e(y)} s_2$ $y = Out(s_1)$ $x = Out(s_2)$ PS-SPEC $j$ ( $j \in x$ ) <span style="margin-left: 20px;"> <math>s_1 \xrightarrow{\epsilon} s_2</math> PS-SPEC <math>k</math> (<math>k \notin x</math>) <math>x = Out(s_2)</math> </span>

Fig. 5. Transition synthesis rules.

uniquely generated for each service primitive  $E_i$  in the rules A2 and B2.

- Step 3 Incorporate the capability of multipath routing into the PE specifications PE-SPEC $i$  constructed in Step 2, such that the resultant specification obeys channel restriction. Next, remove  $\varepsilon$  transitions from PE-SPEC $i$  by the algorithm presented in Ref. [10].
- Step 4 Incorporate the recovery function of rerouting into the protocol specification constructed in Step 3 using timeout event.

### 3.3. Detail of proposed synthesis method

As Steps 1 and 2 are almost the same as those in Ref. [4], we will explain only details of Steps 3 and 4.

#### 3.3.1. Step 3

Step 3 incorporates the capability of multipath routing into  $n$  PE specifications PE-SPECs that obey the channel restriction. This incorporation is executed by applying the following TE procedure. Note that the protocol specification obtained in Step 2 possesses the same graph structures as the service specification, because the transition synthesis rule adds (removes) neither states nor transitions, respectively. That is, each PE-SPEC $i$  has the same number of states and transitions. Hence, for a transition  $(u, E_i, v)$  in S-SPEC, there exists  $n$  transitions such that  $(u, E_i, !e(j), v) \in T_{ip}$ ,  $(u, ?e(i), v) \in T_{jp}$ , and  $n - 2$  transitions  $(u, \varepsilon, v) \in T_{kp}$  ( $k \neq i, j$ ). TE procedure is applied to such  $n$  transitions.

#### TE procedure

Input PE-SPECs obtained in Step 2, and topology graph  $G = (V, E)$ .

Output PE-SPECs with the capability of multipath routing that obeys channel restriction.

#### Procedure

For each  $n$  transition  $(u, E_i, !e(j), v) \in T_{ip}$ ,  $(u, ?e(i), v) \in T_{jp}$ , and  $n - 2$  transitions  $(u, \varepsilon, v) \in T_{kp}$  ( $k \neq i, j$ ,  $1 \leq k \leq n$ ), execute TE-Step 1 through TE-Step 4. Then, remove all  $\varepsilon$  transitions using the algorithm presented in Ref. [10].

#### TE-Step 1

Search all loop-free paths  $\rho_1, \rho_2, \dots, \rho_m$  from  $PE_i$  to  $PE_j$  based on  $G$ .

#### TE-Step 2

If  $(i, j) \notin E$ , remove transitions  $(u, E_i, !e(j), v)$  and  $(u, ?e(i), v)$  from  $T_{ip}$  and  $T_{jp}$ , respectively.

#### TE-Step 3

For each  $\rho \in \{\rho_1, \rho_2, \dots, \rho_m\} - \{\rho_d\}$ , where  $\rho_d$  is a path from  $PE_i$  to  $PE_j$  having no  $R$ -nodes, execute TE-Substeps 3.1 and 3.2.

#### TE-Substep 3.1

For each  $T_{kp}$  ( $k \neq i, j$ ), such that  $PE_k$  is an  $R$ -node on  $\rho$ , remove  $(u, \varepsilon, v)$  from  $T_{kp}$ .

#### TE-Substep 3.2

Add several transitions for each PE based on  $\rho$  as follows:

1. For an adjacent node  $PE_x$  of  $PE_i$  on  $\rho$  ( $PE_i$  is a  $S$ -node on  $\rho$ ), add a transition  $(u, E_i, ?e(x), v)$  to  $T_{ip}$ .
2. For an adjacent node  $PE_y$  of  $PE_j$  on  $\rho$  ( $PE_j$  is a  $D$ -node on  $\rho$ ), add a transition  $(u, ?e(y), v)$  to  $T_{jp}$ .
3. For each  $T_{kp}$  ( $k \neq i, j$ ) such that  $PE_k$  is an  $R$ -node on  $\rho$ , and  $PE_z$  and  $PE_w$  are a pair of adjacent nodes of  $PE_k$ , add a transition  $(u, ?e(z), !e(w), u)$  to  $T_{kp}$ , where  $PE_z$  is on the sub-path of  $\rho$  from  $PE_i$  to  $PE_k$ , and  $PE_w$  is on the sub-path of  $\rho$  from  $PE_k$  to  $PE_j$ .

TE-Step 4 Introduce t-set into PE-SPEC as follows:

1. In the  $T_{ip}$ , remove transitions  $(u, E_i, !e(x_1), v), \dots, (u, E_i, !e(x_m), v)$ . Next, create a new state  $u'$  in  $S_{ip}$ , then add two transitions  $(u, E_i, u')$  and  $(u', !e(t-set), v)$ . Finally, let  $t-set = \{x_1, \dots, x_m\}$ .
2. In the  $T_{jp}$ , remove transitions  $(u, ?e(y_1), v), \dots, (u, ?e(y_m), v)$  and add transition  $(u, ?e(t-set), v)$ . Next, let  $t-set = \{y_1, \dots, y_m\}$ .
3. In the  $T_{kp}$  such that  $PE_k$  is an  $R$ -node on a path  $\rho \in \{\rho_1, \dots, \rho_m\}$ , remove all transitions  $(u, ?e(z_1), !e(w_1), u), \dots, (u, ?e(z_{m'}), !e(w_{m'}), u)$  and add transitions  $(u, ?e(t-set1), !e(t-set2), v)$ . Then, let  $t-set1 = \{z_1, \dots, z_{m'}\}$  and  $t-set2 = \{w_1, \dots, w_{m'}\}$ . Here,  $1 \leq m' \leq m$ .

At TE-Step 1, loop-free communication paths from the  $S$ -node to the  $D$ -node for the message are searched as much as possible by the conventional path enumeration method [11]. At TE-Step 2, transitions that violate channel restriction are removed. If  $\rho_d$  exists in  $G$ , it is clear that the transitions  $(u, E_i, !e(j), v) \in T_{ip}$  and  $(u, ?e(i), v) \in T_{jp}$  obey the channel restriction. It is not necessary to execute TE-Step 2 and TE-Substeps 3.1 and 3.2 for  $\rho_d$ . In TE-Step 4, modification of the  $S$ -node is done to avoid transmission of  $E_i$  more than once.

#### 3.3.2. Step 4

In this step, we incorporate the function of rerouting into PE specifications PE-SPECs obtained in Step 3. When a communication channel fails, a PE at the source node finds the failure by the timeout event, and retransmits messages for rerouting.

When a channel failure occurs on a path and a transmitted message is lost, reception events are not executable in PEs on the path. This is because the source node waits continuously for receiving an acknowledgement of the transmitted message. Hence, we add transitions for retransmission of the message to the source node. However, as a side effect, unspecified receptions may occur. Therefore, we add supplementary transitions so that unspecified receptions are avoided.

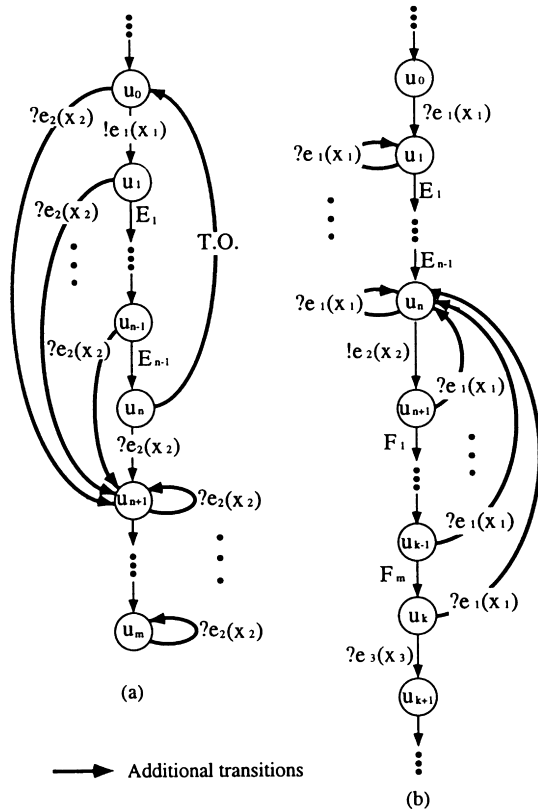


Fig. 6. Addition of transitions in Step 4.

The procedure of Step 4 consists of the following steps S1, S2 and S3: For each transition sequence from an initial state  $u_{init}$  to a final state in each PE-SPEC, we apply steps S1–S3 in this order.

- S1: First, we search a transition  $(u_0, E, u_1)$  such that  $E$  is either a transmission event or a reception event and all transitions from  $u_{init}$  to  $u_0$  are service primitives.
- S2: Here, we consider two cases:  $E = !e_1(x_1)$  and  $E = ?e_1(x_1)$ .

(Case of  $E = !e_1(x_1)$ )

Assume that the event  $(u_n, ?e_2(x_2), u_{n+1})$  is the first reception event in the transition sequence from  $u_0$ . Then, we add the transitions (1), (2) and (3) to PE-SPECi as shown in Fig. 6(a).

1.  $(u_n, T.O., u_0)$ .
2.  $(u_0, ?e_2(x_2), u_{n+1}), (u_1, ?e_2(x_2), u_{n+1}), \dots, (u_{n-1}, ?e_2(x_2), u_{n+1})$ .
3.  $(v, ?e_2(x_2), v)$  for each state  $v$  included in the transition sequence from  $u_n$  to the final state  $u_m$ .

After this, we regard  $u_{n+1}$  as  $u_{init}$ .

(Case of  $E = ?e_1(x_1)$ )

Assume that the event  $(u_k, ?e_3(x_3), u_{k+1})$  is the first reception event in the execution sequence from  $u_1$ . Then, we perform the following (see Fig. 6(b)).

Assume that the event  $(u_n, !e_2(x_2), u_{n+1})$  is the first transmission event in the transition sequence from state  $u_1$  to  $u_k$ . (If the transition is not found, we regard  $u_n$  as  $u_k$ .) Next, we add the following transitions (1) and (2) to PE-SPECi. (If  $u_n = u_k$ , we only add a transition (a).)

1.  $(u_1, ?e_1(x_1), u_1), (u_2, ?e_1(x_1), u_2), \dots, (u_n, ?e_1(x_1), u_n)$ .
2.  $(u_{n+1}, ?e_1(x_1), u_n), (u_{n+2}, ?e_1(x_1), u_n), \dots, (u_k, ?e_1(x_1), u_n)$ .

After this, we regard  $u_k$  as  $u_{init}$ .

S3: We recursively execute S1 and S2 from the new  $u_{init}$ .

#### 4. Correctness of the synthesis method

In this section, we discuss the correctness of the proposed method. For this purpose, we must prove that the obtained protocol specification satisfies Requirements 1 and 2. However, correctness for Requirement 1 can be proved easily because the method is almost the same as the previous method [4]. Then, we omit the proof for Requirement 1 in

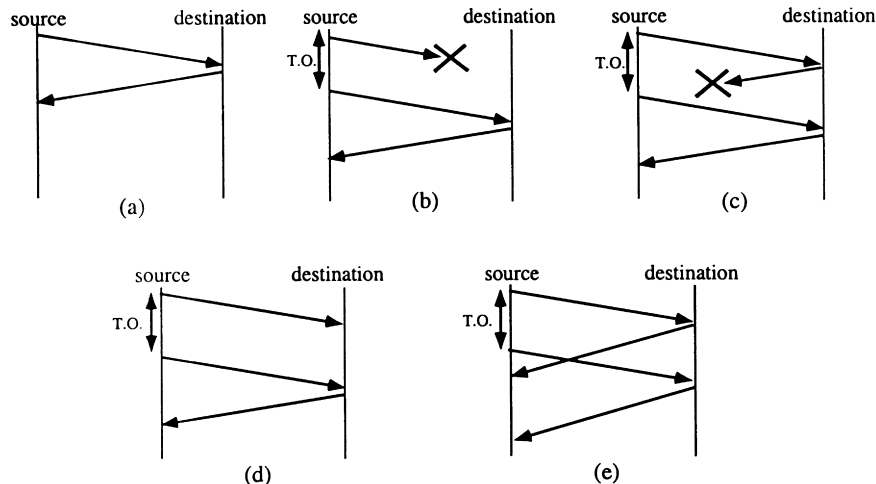


Fig. 7. Sequences for five cases.

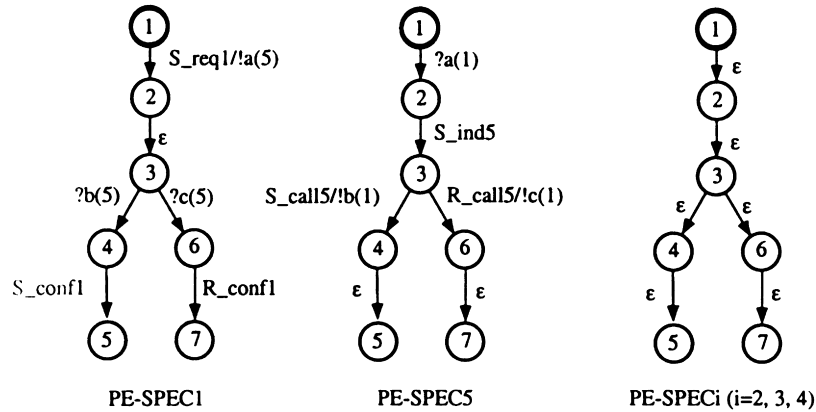


Fig. 8. Protocol specification PE-SPEC<sub>i</sub> after Step 2.

this paper. For the proof for Requirement 2, we must show that the obtained protocol specification satisfies Conditions 1, 2 and 3, even when additional transitions in Step 4 are executed. As it is obvious that protocol specification satisfies Condition 3, we discuss Conditions 1 and 2 here.

Cases shown in Fig. 6(a) and (b) are considered for the source node and destination node, respectively. The timeout events in the source node can occur when a predetermined time elapses. If a message from the source node to the destination node is lost or an acknowledgement message from the destination node is lost, the timeout event can surely occur and the message retransmitted. If the predetermined time for timeout is smaller than the sum of the time for delivery of the message and the time for delivery of the acknowledgement message, then the timeout event possibly occurs and unnecessary retransmission may be executed.

Depending on the loss of the message and its acknowledgement message and on the inappropriate predetermined time for the timeout, all possible cases are divided into the following five cases as shown in Fig. 7:

Case 1 (see Fig. 7(a))

The message from the source node was delivered to the destination node, and the acknowledgement message was also delivered without message loss. Thus, both the transitions from  $u_0$  to  $u_{n+1}$  through  $E_1, \dots, E_{n-1}$  in the source node (shown in Fig. 6(a)) and the transitions from  $u_0$  to  $u_k$  through  $E_1, \dots, E_{n-1}, F_1, \dots, F_m$  in the destination node (shown in Fig. 6(b)) are executed. This case is included in the proof for Requirement 1.

Case 2 (see Fig. 7(b))

After the timeout event occurs due to the loss of the message from the source node, the message is retransmitted. As shown in Fig. 6(a), in the source node after the transitions from  $u_0$  to  $u_n$  through  $E_1, \dots, E_{n-1}$  are executed, the timeout event occurs and the transitions from  $u_0$  to  $u_{n+1}$  through  $E_1, \dots, E_{n-1}$  are executed. That is, message  $e_1$  is retransmitted in the source node. Execution of transitions in the destination node is the same as that in Case 1.

Case 3 (see Fig. 7(c))

After the timeout event occurs due to the loss of the acknowledgement message from the destination node, the message is retransmitted from the source node. As shown in Fig. 6(a), the execution of transitions in the source node is the same as that in Case 2. On the contrary, as shown in Fig. 6(b), in the destination node after transitions from  $u_0$  to  $u_k$  through  $E_1, \dots, E_{n-1}, F_1, \dots, F_m$  are executed, the event  $?e_1(x_1)$  occurs and then the transitions from  $u_n$  to  $u_k$  through  $E_1, \dots, E_{n-1}, F_1, \dots, F_m$  are executed.

Case 4 (see Fig. 7(d))

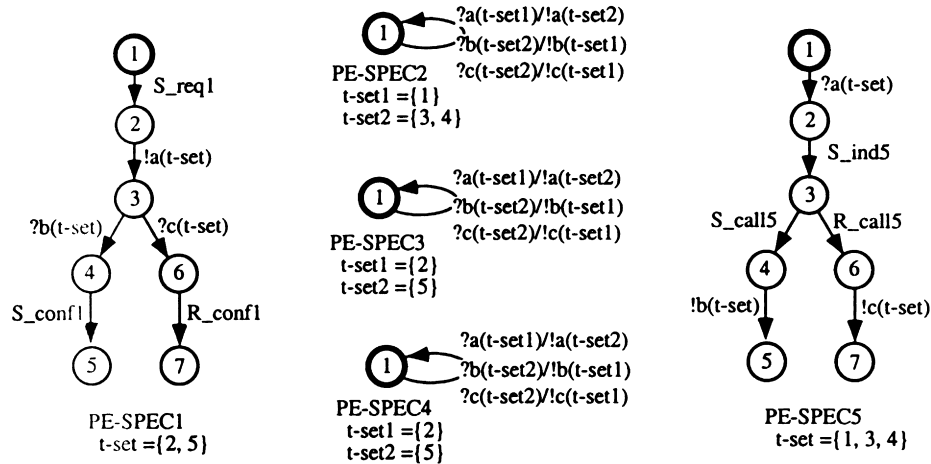
There is no loss of message and its acknowledgement message. However, due to inappropriate predetermined time for the timeout event, the message is retransmitted. After the transmitted and retransmitted messages are received, the acknowledgement message is transmitted. In Fig. 6, transitions for avoiding unspecified reception are added for the source and destination nodes.

In the source node (as shown in Fig. 6(a)), after transitions from  $u_0$  to  $u_n$  through  $E_1, \dots, E_{n-1}$  are executed, the timeout event and the reception event  $?e_2(x_2)$  occur in this order. Message  $e_2$  can be received at a state between  $u_0$  and  $u_n$ . In the destination node (as shown in Fig. 6(b)), after message  $e_1$  is received by executing the reception event  $?e_1(x_1)$ , the same message  $e_1$  is received at a state between  $u_0$  and  $u_n$ . Then, transitions from  $u_n$  to  $u_k$  are executed through  $F_1, \dots, F_m$ .

Case 5 (see Fig. 7(e))

The situation is the same as that in Case 4 with respect to no loss of the message and its acknowledgement, and inappropriate predetermined time for the timeout event. However, the acknowledgement message is transmitted twice from the destination node, as the acknowledgement is transmitted before the retransmitted message is received. In Fig. 6, transitions for avoiding unspecified messages are also added for the source and destination nodes.

In the source node (as shown in Fig. 6(a)), the reception event  $?e_2(x_2)$  is executed at a state between  $u_{n+1}$  and  $u_m$  after execution of transitions mentioned in Case 4. In the destination node (as shown in Fig. 6(b)), after transitions

Fig. 9. Protocol specification PE-SPEC $i$  after Step 3.

from  $u_0$  to  $u_{n+1}$  are executed, the reception event  $?e_1(x_1)$  occurs at a state between  $u_n$  and  $u_k$ . After this, transitions from  $u_n$  to  $u_{k+1}$  are executed through  $F_1, \dots, F_{n-1}$ .

In Case 1, the execution order of primitives is executed in such an order that primitives in  $F_1, \dots, F_m$  are executed after all primitives in  $E_1, \dots, E_{n-1}$  are executed. This is required in the given service specification. Although redundant primitives are executed in Cases 2–5, the above execution order of primitives in Case 1 is also kept in Cases 2–5.

Based on the above observation, we can say that Conditions 1 and 2 are satisfied in the synthesized protocol specification.

## 5. Example

### 5.1. Explanation of the synthesis method by example

We apply our synthesis method to a typical example. Consider a service specification S-SPECs shown in Fig. 3 and a topology graph  $G$  shown in Fig. 2.

At Step 1, service primitives are projected to PS-SPEC1, PS-SPEC2, PS-SPEC3, PS-SPEC4, and PS-SPEC5. At Step 2, PE specifications PE-SPECs are obtained from PS-SPECs. The synthesis rules satisfy Condition 1. For example, consider transition  $(1, S\_req1, 2)$  in PS-SPEC1 and transition  $(1, \varepsilon, 2)$  in PS-SPEC $i$  ( $i = 2, 3, 4, 5$ ). For this case, as  $OUT(2) = \{5\} \neq \{1\}$  (see Fig. 3), the transition synthesis rule A2 and B2 are applied (see Fig. 5). As a result, two transitions  $(1, S\_req1, 2)$  in PS-SPEC1 and  $(1, \varepsilon, 2)$  in PS-SPEC5 are changed to  $(1, S\_req1!a(5), 2)$  and  $(1, ?a(1), 2)$ , respectively. However,  $(1, \varepsilon, 2)$  in PS-SPEC $i$  ( $i = 2, 3, 4$ ) remains unchanged as  $\{2, 3, 4\} \neq OUT(2)$  for PS-SPEC $i$  ( $i = 2, 3, 4$ ). Fig. 8 shows the result of Step 2.

Step 3 constructs PE-SPECs with multipath transmission that obey the channel restriction. For example, consider

transmission  $(1, S\_req1!a(5), 2)$  in PE-SPEC1,  $(1, ?a(1), 2)$  in PE-SPEC5,  $(1, \varepsilon, 2)$  in PS-SPEC $i$  ( $i = 2, 3, 4$ ) in Fig. 8. There are three paths from node 1 (PE $_1$ ) to node 5 (PE $_5$ ) in  $G$  (see Fig. 2),  $\rho_1: PE_1 \rightarrow PE_5$ ,  $\rho_2: PE_1 \rightarrow PE_2, \rightarrow PE_3, \rightarrow PE_5$ ,  $\rho_3: PE_1 \rightarrow PE_2, \rightarrow PE_4, \rightarrow PE_5$ . Next, with respect to  $\rho_1$ , transitions  $(1, S\_req1!a(5), 2)$ ,  $(1, ?a(1), 2)$  are unchanged in PS-SPEC $i$  ( $i = 1, 5$ ), as  $\rho_1$  has no  $R$ -node. For  $\rho_2$ , transitions  $(1, S\_req1!a(2), 2)$ ,  $(1, ?a(1)!a(3), 1)$ ,  $(1, ?a(2)!a(5), 1)$ ,  $(1, ?a(3), 2)$  are added to PS-SPEC $i$  ( $i = 1, 2, 3, 5$ ) by TE-Substep 3.2, the transitions in PS-SPEC $_1$  are modified to transitions  $(1, S\_req1, 1')$ , respectively. Similarly, for  $\rho_3$ , transitions  $(1, S\_req1!a(2), 2)$ ,  $(1, ?a(1)!a(4), 1)$ ,  $(1, ?a(2)!a(5), 1)$ ,  $(1, ?a(4), 2)$  are added to PS-SPEC $i$  ( $i = 1, 2, 4, 5$ ) by TE-Substep 3.2, the transitions in PS-SPEC $_1$  are modified to transitions  $(1, S\_req1, 1')$ , respectively. Then, the transitions in PE-SPEC1 are modified to  $(1', !a(t-set), 2)$ , where  $t-set = \{2, 5\}$ . Similarly, the transitions in PE-SPEC5 are modified to  $(1, ?a(t-set), 2)$ , where  $t-set = \{1, 3, 4\}$ . And the transitions in PE-SPEC2 are modified to  $(1, ?a(t-set1)!a(t-set2), 1)$ , where  $t-set1 = \{1\}$  and  $t-set2 = \{3, 4\}$ . Other transitions in PE-SPEC3 and PE-SPEC4 are similarly modified, and all  $\varepsilon$  transitions are removed. Fig. 9 shows a protocol specification PE-SPECs after Step 3.

In Step 4, timeout events and some other transitions are added. For example, consider execution sequence  $S\_req1, !a(t-set), ?b(t-set), S\_conf1$  in PE-SPEC1. As transition  $(3, ?b(t-set), 4)$  exists after transition  $(2, !a(t-set), 3)$  on the transition sequence, four transitions  $(3, T.O., 2)$ ,  $(2, ?b(t-set), 4)$ ,  $(4, ?b(t-set), 4)$ ,  $(5, ?b(t-set), 5)$  are added in PE-SPEC1. Fig. 10 shows the final protocol specification after Step 4, where each number in circle is renumbered.

### 5.2. Fault-tolerance of synthesized routing protocol

In this subsection, we discuss whether the protocol specification obtained by our method realizes both Requirements 1 and 2 or not. Consider the protocol specification shown in



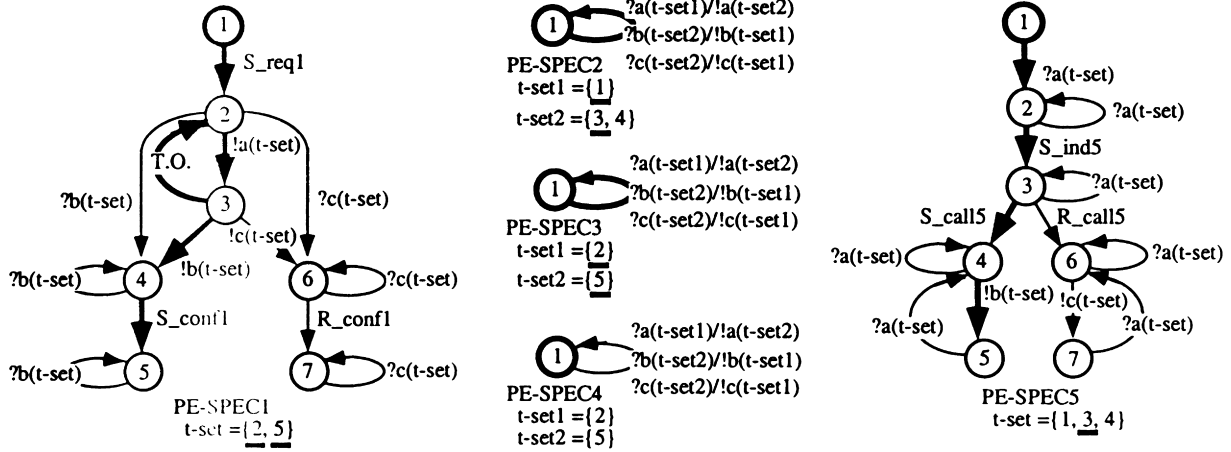


Fig. 10. Final protocol specification after Step 4.

Fig. 10, and assume that the channel between PE<sub>1</sub> and PE<sub>5</sub> in Fig. 2 fails.

First PE<sub>1</sub> delivers directly message *a* through the channel between PE<sub>1</sub> and PE<sub>5</sub>. However, this message is lost because of the channel failure. Then PE<sub>1</sub> can know that the message is lost by the timeout event. Next, the PE<sub>1</sub> retransmits the message via another path. Let us consider the following path: PE<sub>1</sub> → PE<sub>2</sub> → PE<sub>3</sub> → PE<sub>5</sub>. This retransmission is realized by executing transitions *!a*(*t-set*) in PE-SPEC1, *?a*(*t-set*1)/!*a*(*t-set*2) in PE-SPEC2, *?a*(*t-set*1)/!*a*(*t-set*2) in PE-SPEC3, and *?a*(*t-set*) in PE-SPEC5. Here, *t-set* and *t-set*2 are interpreted as follows. Based on the source based routing policy in Section 2.4, e.g. *!a*(2) is actually executed for *!a*(*t-set*) in PE-SPEC1, and *!a*(3) is actually executed for *!a*(*t-set*2) in PE-SPEC2.

It is clear that for the channel failure between PE<sub>1</sub> and PE<sub>5</sub>, the execution order of service primitives is kept in the transmission sequence denoted by bold arrows in Fig. 10.

## 6. Discussion

### 6.1. Flexibility for topology change

In this subsection, we describe only a procedure that realizes Requirement 3. At first, we explain the case of  $G + \Delta G$  (i.e. some PEs are added). We suppose that PEs and their associated channels are incrementally added. In order to satisfy Requirement 3, we define a new problem FT as follows:

**Problem FT. Input:** (1) A protocol specification, which is obtained from Protocol Synthesis Problem (by applying our proposed method to a topology graph  $G$  with Restriction 1, and a service specification  $S$  with Restrictions 2 and 3. (2) Topology change  $\Delta G$  due to addition or deletion of a node and its associated channels. We assume that the updated graph  $G + \Delta G$  or  $G - \Delta G$  still satisfies Restriction 1.

**Output:** A protocol specification, which is obtained by

applying our synthesis method to the topology graph  $G + \Delta G$  or  $G - \Delta G$  and a service specification  $S$ .

In this problem FT, we discuss the process of realizing or obtaining the output, and show that the proposed method attains it effectively using *t-set*.

Assume that PE<sub>*i*</sub> is a newly added node and PE<sub>*j*</sub><sub>1</sub>, PE<sub>*j*</sub><sub>2</sub>, ..., PE<sub>*j*</sub><sub>*k*</sub> are connected to PE<sub>*i*</sub> as shown in Fig. 11. These are the elements of  $\Delta G$ . The added PE<sub>*i*</sub> can be *R-node*. Then, let PE<sub>*j*</sub><sub>*p*</sub> and PE<sub>*j*</sub><sub>*q*</sub> ( $1 \leq p \leq k, 1 \leq q \leq k, p \neq q$ ) are arbitrary two PEs among PE<sub>*j*</sub><sub>1</sub>, PE<sub>*j*</sub><sub>2</sub>, ..., PE<sub>*j*</sub><sub>*k*</sub>. There exist loop-free directed paths from *S-node* to *D-node* through PE<sub>*j*</sub><sub>*p*</sub> and PE<sub>*j*</sub><sub>*q*</sub> in  $G$ . For the PEs on these paths, transitions for message delivery were specified in PE-SPECs. By adding PE<sub>*i*</sub> and channels (*i*,*j*<sub>*p*</sub>), (*i*,*j*<sub>*q*</sub>), new loop-free directed paths, each of which consists of a subpath from *S-node* to PE<sub>*j*</sub><sub>*p*</sub>, a subpath (*j*<sub>*p*</sub>,*i*), (*i*,*j*<sub>*q*</sub>), and a subpath from PE<sub>*j*</sub><sub>*q*</sub> to *D-node*, appear in  $G + \Delta G$ . As, for the PEs on the subpath from *S-node* to PE<sub>*j*</sub><sub>*p*</sub> and the subpath from PE<sub>*j*</sub><sub>*q*</sub> to *D-node*, transitions for message delivery have been specified in PE-SPECs, modification of PE-SPEC is unnecessary for the PEs except for PE<sub>*j*</sub><sub>*p*</sub> and PE<sub>*j*</sub><sub>*q*</sub>. We have only to change, for each message *e*, *!e*(*t-set*<sub>*p*</sub>) in PE-SPEC<sub>*j*</sub><sub>*p*</sub> and *?e*(*t-set*<sub>*q*</sub>) in PE-SPEC<sub>*j*</sub><sub>*q*</sub> into *!e*(*t-set*'<sub>*p*</sub>) where  $t\text{-set}'_p = t\text{-set}_p \cup \{i\}$  and *?e*(*t-set*'<sub>*q*</sub>) where  $t\text{-set}'_q = t\text{-set}_q \cup \{i\}$ , respectively. Similarly, if transition *?e*(*t-set*<sub>*i*</sub>1)/!*e*(*t-set*<sub>*i*</sub>2) does not exist in PE-SPEC<sub>*i*</sub>, then transition *?e*(*t-set*<sub>*i*</sub>1)/!*e*(*t-set*<sub>*i*</sub>2) where  $t\text{-set}_{i1} = \{j_p\}$  and  $t\text{-set}_{i2} = \{j_q\}$  are added. Otherwise, the transition is updated to *?e*( $t\text{-set}_{i1} \cup \{j_p\}$ )/!*e*( $t\text{-set}_{i2} \cup \{j_q\}$ ).

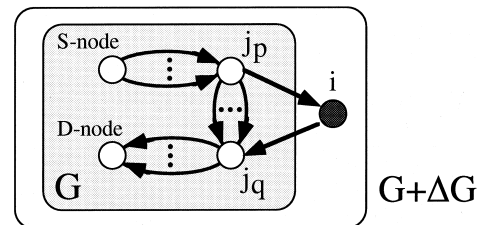


Fig. 11. Concept of PE added.

Next, we explain the case of  $G - \Delta G$ . As deletion of  $S$ -node or  $D$ -node makes message delivery impossible, we assume that the deleted  $PE$  is  $R$ -node. Assume that in Fig. 11  $PE_i$  is a deleted node and that  $PE_i$  was connected to  $PE_{j_1}, PE_{j_2}, \dots, PE_{j_k}$ . By eliminating  $PE_i$  and channels  $(i, j_p), (i, j_q)$ , directed paths  $(j_p, i), (i, j_q)$  are deleted for any  $p$  and  $q$  ( $1 \leq p \leq k, 1 \leq q \leq k, p \neq q$ ). In this case, we have only to delete from  $PE\text{-SPEC}j_p$  index  $i \in t\text{-set}_p$  in  $!e(t\text{-set}_p)$ , and we also delete from  $PE\text{-SPEC}j_q$  index  $i \in t\text{-set}_q$  in  $?e(t\text{-set}_q)$ . Then, we delete  $?e(t\text{-set}_{i_1})/!e(t\text{-set}_{i_2})$  in  $PE\text{-SPEC}i$ .

## 6.2. An extension for multicast routing

Multicast communication services will be one of the most promising future applications, which includes real-time flows, in both the B-ISDN and the Internet [2].

We have proposed an extension of the synthesis method presented in this paper for multicast routing protocols, which are fault-tolerant [12]. The multicast routing protocol is defined to be fault-tolerant if messages can be retransmitted when a message loss occurs. The method generates a multicast routing protocol in consideration of behavior of a copy node. In the protocol, against a message loss, not a source node but a copy node can retransmit the message to destinations. Therefore, the retransmission can be fast.

In order to describe the behavior of a copy node efficiently, we consider two kinds of service specifications. One is a set of service specification between an  $S$ -node and  $Copy$  nodes. Another is a set of service specifications between a  $Copy$  node and  $D$ -nodes. The synthesis method presented in Ref. [12] is applied to both the specifications. Moreover, to handle the synchronization of messages in the copy node efficiently, a *fork state* and a *join state* are introduced into the protocol specification. As a result, several component pieces of protocol specifications are obtained. Finally, a final protocol specification is constructed from these pieces.

## 7. Conclusion

In this paper, we have proposed a new synthesis method which generates a fault-tolerant and flexible multipath routing protocol from a given service specification. The proposed method enables derivation of such a fault-tolerant

protocol specification such that messages are rerouted at the source node and delivered to the destination node even when a communication path fails. Hence, the proposed design method enables the efficient production of reliable fault-tolerant routing protocol specification at a lower cost.

Further, for the given network changes, only PE specifications corresponding to the changes need to be modified in the obtained protocol. Therefore, only a small amount of change is needed for the change of network topology. This is useful for routing protocol for a network with large number of nodes. We also briefly describe an extension of the proposed method for generating multicast routing protocols.

## References

- [1] S. Dolev, J.L. Welch, Crash resilient communication in dynamic networks, *IEEE Transactions on Computers* 46 (1) (1997) 14–26.
- [2] C. Huitema, *Ipv6 The New Internet Protocol*, 2, Prentice Hall, Englewood Cliffs, NJ, 1997.
- [3] Y. Hatanaka, M. Nakamura, Y. Kakuda, T. Kikuno, A synthesis method for fault-tolerant and flexible multipath routing protocols, in: *Proc. IEEE International Conference on Engineering of Complex Computer Systems*, 1997, pp. 96–105.
- [4] Y. Kakuda, M. Nakamura, T. Kikuno, Automated synthesis of protocol specifications with parallelly executable multiple primitives, *IEICE Transactions on Fundamentals* E77-A (10) (1994) 1634–1645.
- [5] R.L. Probert, K. Saleh, Synthesis of communication protocols survey and assessment, *IEEE Transactions on Computers* 40 (4) (1991) 468–476.
- [6] M.T. Liu, *Protocol Engineering*, *Advances in Computers* 29, Academic, New York, 1989 pp. 79–195.
- [7] G. Singh, M. Sammata, On the construction of multiphase communication protocols, in: *Proc. International Conference on Network Protocols*, 1994, pp. 151–158.
- [8] P.M. Chu, M.T. Liu, Protocol synthesis in a state transition model, in: *Proc. International Computer Software and Applications Conference*, 1988, pp. 505–512.
- [9] K. Saleh, R.L. Probert, Automatic synthesis of protocol specifications from service specifications, *Proc. Intl Phoenix Conference on Computers and Communications*, 1991, pp. 615–621.
- [10] J.E. Hopcroft, J.D. Ullman, *Introduction to Automata Theory, Language, and Computation*, Addison-Wesley, Reading, MA, 1979.
- [11] J.V. Leewen, *HandBook of Theoretical Science*, Elsevier, Amsterdam, 1990.
- [12] K. Ishida, K. Amano, A synthesis method for fault-tolerant multicast routing protocol, *Parallel and Distributed Processing* 1388, Springer, Berlin, 1998 pp. 1121–1130.